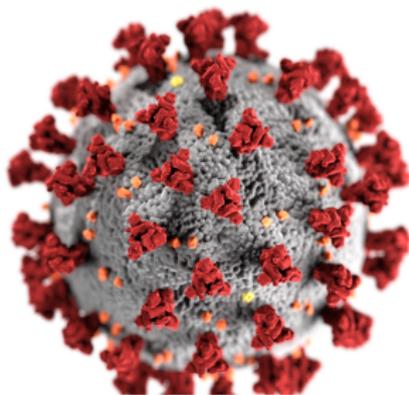


Compressed indexing of (ultra) large viral alignments

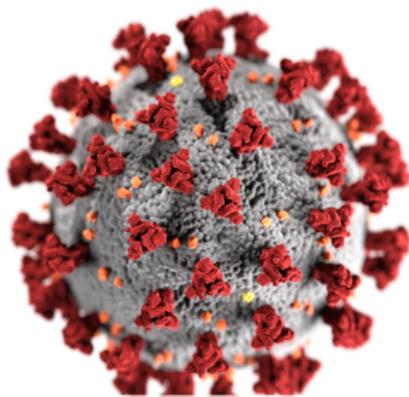
M. Salson, T. Baudeau, A. Boddaert, A. B. Gueye, L. Bulteau,
Y. Hernandez--Courbevoie, C. Marchet, N. Pan, S. Will, Y. Ponty

Characterising SARS-CoV-2 RNA structure



Public domain CDC

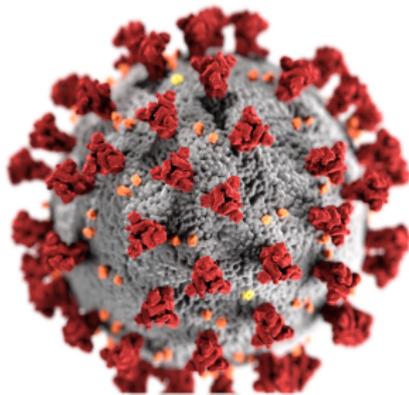
Characterising SARS-CoV-2 RNA structure



Public domain CDC

RNA virus
30 kbp genome

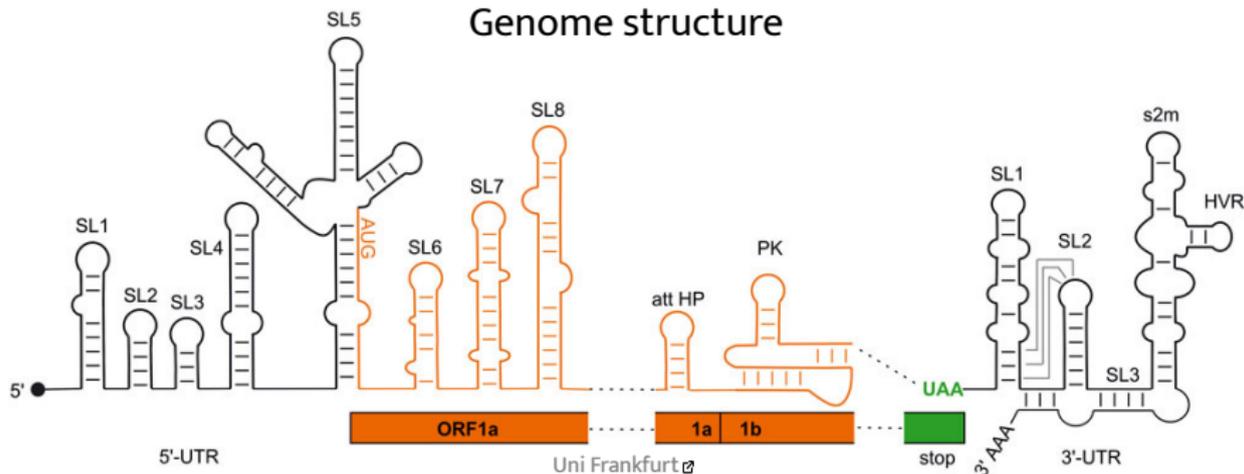
Characterising SARS-CoV-2 RNA structure



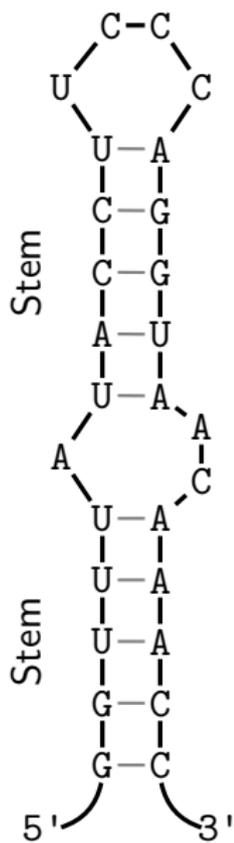
Public domain CDC

RNA virus
30 kbp genome

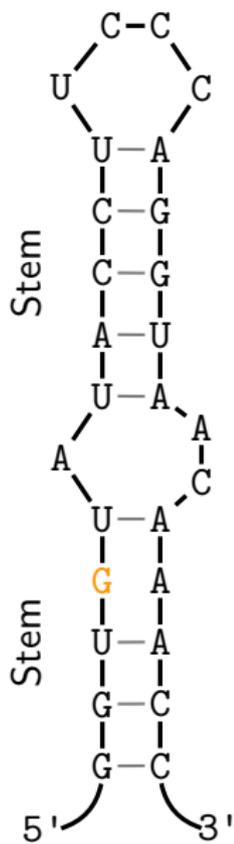
Genome structure



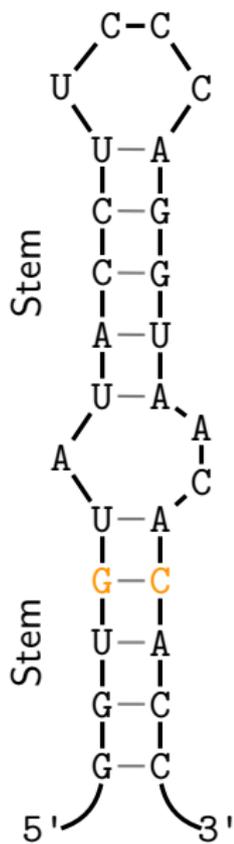
Covariations are a clue to identify stems



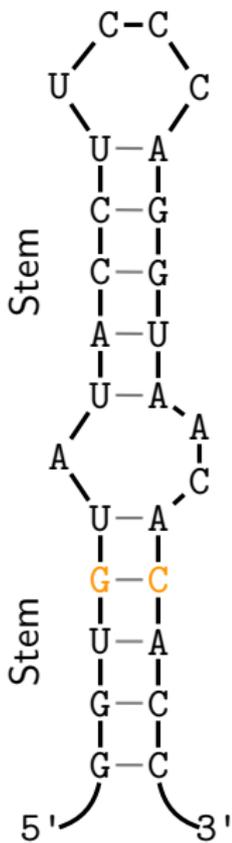
Covariations are a clue to identify stems



Covariations are a clue to identify stems

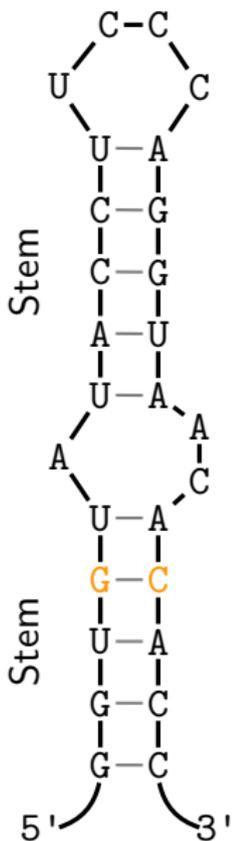


Covariations are a clue to identify stems



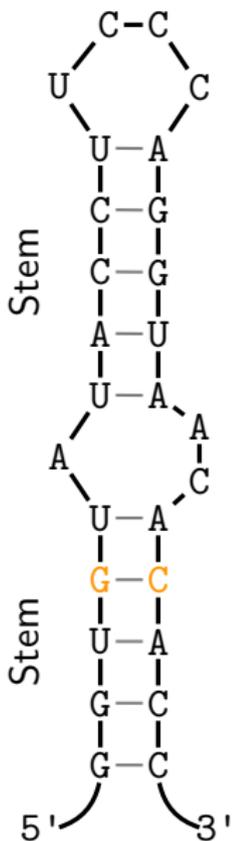
GGUUUAUACCUUCCCAGGUAACAAACC

Covariations are a clue to identify stems



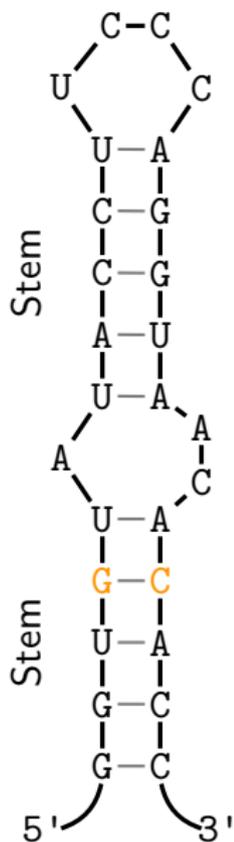
```
GGUUUAUACCUUCCCAGGUAACAAACC  
GGUUUAUACCUUCCCAGGUAACAAACC  
GGUUUAUACCUUCCCAGGUAACAAACC  
GGUUUAUACCUUCCCAGGUAACAAACC  
GGUUUAUACCUUCCCAGGUAACAAACC  
GGUUUAUACCUUCCCAGGUAACAAACC
```

Covariations are a clue to identify stems



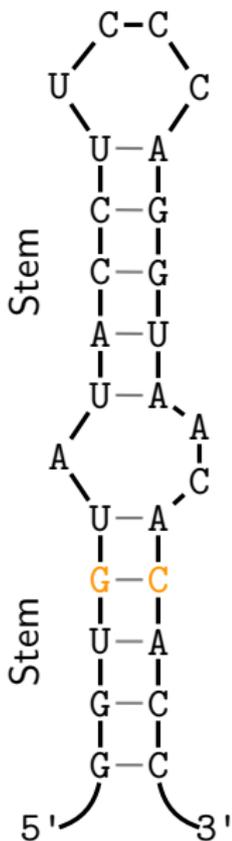
```
GGUUUAUACCUUCCCAGGUAACAAACC  
GGUGUAUACCUUCCCAGGUAACACACC  
GGUUUAUACCUUCCCAGGUAACAAACC  
GGUUUAUACCUUCCCAGGUAACAAACC  
GGUGUAUACCUUCCCAGGUAACACACC  
GGUGUAUACCUUCCCAGGUAACACACC
```

Covariations are a clue to identify stems



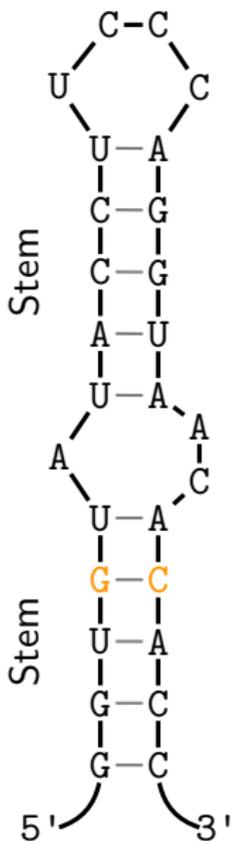
```
GGUUUAUACCUUCGCAGGUAACAAACC  
GGUGUAUACCUUCCCAGGUAACACACC  
GGUUUAUACCUUCCCAGGUAACAAACC  
GGUUUAUACCUUCGCAGGUAACAAACC  
GGUGUAUACCUUCGCAGGUAACACACC  
GGUGUAUACCUUCCCAGGUAACACACC
```

Covariations are a clue to identify stems



GGUUUAUACCUUCGCAGGUAACAAACC
GGUGUAUACCUUCCCAGGUAACAACC
GGUUUAUACCUUCCCAGGUAACAAACC
GGUUUAUACCUUCGCAGGUAACAAACC
GGUGUAUACCUUCGCAGGUAACAACC
GGUGUAUACCUUCCCAGGUAACAACC

Covariations are a clue to identify stems



GGUUUAUACCUUCGCAGGUAACAAACC
GGUGUAUACCUUCCCAGGUAACAACC
GGUUUAUACCUUCCCAGGUAACAAACC
GGUUUAUACCUUCGCAGGUAACAAACC
GGUGUAUACCUUCGCAGGUAACAACC
GGUGUAUACCUUCCCAGGUAACAACC

Covariations

Identifying covariations through conservation scores

| | |
|---|---|
| U | A |
| G | C |
| U | A |
| U | A |
| G | C |
| G | C |

6 compatible pairs

| | |
|---|---|
| U | A |
| G | A |
| G | A |
| U | C |
| G | C |
| U | C |

2 compatible pairs

The conservation score of a pair of columns depends on the number of compatible pairs

See RNAalifold (Bernhart et al, 2008)

With n columns of size s , this could be computed in $\Theta(sn^2)$

Lots of data to identify covariations in SARS-CoV-2

3,079,138

genomes

On NCBI Virus, as of 26 Nov 2024 [↗](#)

Awesome! But that's quite a MSA...

Assuming we can build it...

Computing conservation scores on millions of genomes

Let's assume we have a MSA of 1M SARS-CoV-2

Computing conservation scores on millions of genomes

Let's assume we have a MSA of 1M SARS-CoV-2

- ▶ That's 30k columns of 1Mbp

Computing conservation scores on millions of genomes

Let's assume we have a MSA of 1M SARS-CoV-2

- ▶ That's 30k columns of 1Mbp
- ▶ We need to consider every pair of columns
→ 450 M pairs of columns

Computing conservation scores on millions of genomes

Let's assume we have a MSA of 1M SARS-CoV-2

- ▶ That's 30k columns of 1Mbp
- ▶ We need to consider every pair of columns
→ 450 M pairs of columns
- ▶ 10^{14} pairs of nucleotides must be considered

Computing conservations scores on millions of genomes

Let's assume we have a MSA of 1M SARS-CoV-2

- ▶ That's 30k columns of 1Mbp
- ▶ We need to consider every pair of columns
→ 450 M pairs of columns
- ▶ 10^{14} pairs of nucleotides must be considered

More generally, getting any kind of information from a 1Mbp column is inefficient

A self-index for multiple sequence alignment (MSA)

GGUUUAUACCUUCGCAGGUAACAAACC
GGUGUAUACCUUCCCAGGUAACACACC
GGUUUAUACCUUCCCAGGUAACAAACC
GGUUUAUACCUUCGCAGGUAACAAACC
GGUGUAUACCUUCGCAGGUAACACACC
GGUGUAUACCUUCCCAGGUAACACACC

A self-index for multiple sequence alignment (MSA)

GGUUUAUACCUUCGCAGGUAACAAACC
GGUGUAUACCUUCCAGGUAACACACC
GGUUUAUACCUUCCAGGUAACAACC
GGUUUAUACCUUCGCAGGUAACAAACC
GGUGUAUACCUUCGCAGGUAACACACC
GGUGUAUACCUUCCAGGUAACACACC

A self-index for multiple sequence alignment (MSA)

GGUUUAUACCUUCGCAGGUAACAAACC

GGUGJAUACCUUCCAGGUAACACACC

GGUUUAUACCUUCCCAGGUAACAACC

GGUUUAUACCUUCGCAGGUAACAAACC

GGUGJAUACCUUCGCAGGUAACACACC

GGUGJAUACCUUCCAGGUAACACACC

11111111111111111111111111111111

0001000000000100000000001000

000100000000000000000000001000

000000000000000100000000000000

00010000000000000000000000001000

000000000000000100000000000000

Bit vectors
are stored
column-
wise

A self-index for multiple sequence alignment (MSA)

GGUUUAUACCUUCGCAGGUAACAAACC

GGUGUAUACCUUCCAGGUAACACACC

GGUUUAUACCUUCCCAGGUAACAACC

GGUUUAUACCUUCGCAGGUAACAAACC

GGUGUAUACCUUCGCAGGUAACACACC

GGUGUAUACCUUCCAGGUAACACACC

11111111111111111111111111111111

0001000000000100000000001000

00010000000000000000000001000

000000000000000100000000000000

000100000000000000000000001000

000000000000000010000000000000

GGUUUAUACCUUCGCAGGUAACAAACC

G
U
G

C
G
C

C
A
C

Bit vectors
are stored
column-
wise

A self-index for multiple sequence alignment (MSA)

r_i : number of runs of an identical letter in column i of the MSA

r_j : number of 1s in the bit vector of column i

11111111111111111111111111111111

0001000000000100000000001000

000100000000000000000000001000

000000000000000100000000000000

000100000000000000000000001000

000000000000000100000000000000

GGUUUAUACCUUCGCAGGUAACAAACC

G
U
G

C
G
C

C
A
C

Bit vectors
are stored
column-
wise

rank and select for querying our self-index for MSA

rank/select are fundamental operations on bit vectors

$\text{rank}(B, i)$: nb of 1s in $B[0 \dots i]$
 $\text{select}(B, i)$: position of the i -th 1 in B

rank and select for querying our self-index for MSA

rank/select are fundamental operations on bit vectors

$\text{rank}(B, i)$: nb of 1s in $B[0 \dots i]$
 $\text{select}(B, i)$: position of the i -th 1 in B

1

0

0

0

1

0

1

0

rank and select for querying our self-index for MSA

rank/select are fundamental operations on bit vectors

$\text{rank}(B, i)$: nb of 1s in $B[0 \dots i]$
 $\text{select}(B, i)$: position of the i -th 1 in B

1
0
0
0
1
0 → rank: 2
1
0

rank and select for querying our self-index for MSA

rank/select are fundamental operations on bit vectors

$\text{rank}(B, i)$: nb of 1s in $B[0 \dots i]$
 $\text{select}(B, i)$: position of the i -th 1 in B

1
0
0
0
select(2) \longrightarrow 1
0 \longrightarrow rank: 2
1
0

rank and select for querying our self-index for MSA

rank/select are fundamental operations on bit vectors

$\text{rank}(B, i)$: nb of 1s in $B[0 \dots i]$
 $\text{select}(B, i)$: position of the i -th 1 in B

Compressed bit-vectors can support
constant-time rank/select operations

See eg. Gog et al, 2014

Querying CREMSA

B

nt

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | | |
|---|-----------------------------|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|--|
| 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | | |
| 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | |
| 2 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| 4 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | |
| 5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| | GGUUUAUACCUUCGCAGGUAACAAACC | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | G | | | | | | | | | | | | | C | | | | | | | | | | | | C | | |
| | | U | | | | | | | | | | | | | G | | | | | | | | | | | | | A | |
| | | G | | | | | | | | | | | | | C | | | | | | | | | | | | | C | |

Querying CREMSA

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | |
|----|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|--|
| 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | |
| 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | |
| 2 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| 4 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | |
| 5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| nt | | | | G | | | | | | | | | | C | | | | | | | | | | | | | | |
| | | | | U | | | | | | | | | | G | | | | | | | | | | | | | | |
| | | | | G | | | | | | | | | | C | | | | | | | | | | | | | | |

Accessing $s_i[j]$

Querying CREMSA

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | |
| 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| 2 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 4 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| 5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| nt | | | | G | | | | | | | | | | C | | | | | | | | | | | | | | C |
| | | | | U | | | | | | | | | | G | | | | | | | | | | | | | | A |
| | | | | G | | | | | | | | | | C | | | | | | | | | | | | | | C |

Accessing $s_i[j]$

$s_2[13]$?

Querying CREMSA

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | |
|----------|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|--|
| 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | |
| 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | |
| <i>B</i> | 2 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | |
| | 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| | 4 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | |
| | 5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| nt | | | | G | | | | | | | | | C | | | | | | | | | | C | | | | | |
| | | | | U | | | | | | | | | G | | | | | | | | | | A | | | | | |
| | | | | G | | | | | | | | | C | | | | | | | | | | C | | | | | |

Accessing $s_i[j]$

$s_2[13]$?

Querying CREMSA

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----------|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|--|
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | | |
| 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | |
| 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | |
| <i>B</i> | 2 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| | 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| | 4 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | |
| | 5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| nt | | | | | G | | | | | | | | | C | | | | | | | | | | | | | | | |
| | | | | | U | | | | | | | | | G | | | | | | | | | | | | | | | |
| | | | | | G | | | | | | | | | C | | | | | | | | | | | | | | | |

Accessing $s_i[j]$

$s_2[13]$?

Querying CREMSA

| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | |
|----------|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|
| <i>B</i> | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| | 2 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| | 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | 4 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 |
| | 5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| nt | | | | | G | | | | | | | | | C | | | | | | | | | | | | | | C |
| | | | | | U | | | | | | | | | G | | | | | | | | | | | | | | A |
| | | | | | G | | | | | | | | | C | | | | | | | | | | | | | | C |

Accessing $s_i[j]$

$$s_i[j] = nt_j[\text{rank}(B_j, i)]$$

$$\Theta(1)$$

Querying CREMSA

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|-----------|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | |
| <i>B</i> | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| | 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| | 2 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| | 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| | 4 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| | 5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| <i>nt</i> | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
| | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
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Accessing $s_i[j]$

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Iterating on 1s (with
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Querying CREMSA

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Accessing $s_i[j]$

$$s_i[j] = nt_j[\text{rank}(B_j, i)]$$

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Querying CREMSA

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| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | |
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| 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 2 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 4 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| nt | | | | G | | | | | | | | | | C | | | | | | | | | | | | | | C |
| | | | | U | | | | | | | | | | G | | | | | | | | | | | | | | A |
| | | | | G | | | | | | | | | | C | | | | | | | | | | | | | | C |

Accessing $s_i[j]$

$$s_i[j] = nt_j[\text{rank}(B_j, i)]$$

$\Theta(1)$

Counting nt in col. j

Iterating on 1s (with select) to compute the length of each run

| | | | |
|---|---|---|---|
| A | C | G | T |
| 0 | 2 | 3 | 0 |

Querying CREMSA

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | |
| 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 2 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 4 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 |
| 5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| nt | | | | G | | | | | | | | | | C | | | | | | | | | | | | | | C |
| | | | | U | | | | | | | | | | G | | | | | | | | | | | | | | A |
| | | | | G | | | | | | | | | | C | | | | | | | | | | | | | | C |

Accessing $s_i[j]$

Counting nt in col. j

$$s_i[j] = nt_j[\text{rank}(B_j, i)]$$

$\Theta(1)$

| | | | |
|---|---|---|---|
| A | C | G | T |
| 0 | 3 | 3 | 0 |

Querying CREMSA

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | |
| 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 2 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 4 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| nt | | | | G | | | | | | | | | | | C | | | | | | | | | | | | | C |
| | | | | U | | | | | | | | | | | G | | | | | | | | | | | | | A |
| | | | | G | | | | | | | | | | | C | | | | | | | | | | | | | C |

Accessing $s_i[j]$

Counting nt in col. j

$$s_i[j] = nt_j[\text{rank}(B_j, i)]$$

$$\Theta(1)$$

$$\Theta(r_j)$$

Querying CREMSA

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|----|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|--|
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | | |
| 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | |
| 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | |
| 2 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| 4 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | |
| 5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | |
| nt | | | | G | | | | | | | | | | C | | | | | | | | | | | | | C | | |
| | | | | U | | | | | | | | | | G | | | | | | | | | | | | | | A | |
| | | | | G | | | | | | | | | | C | | | | | | | | | | | | | | C | |

Accessing $s_i[j]$

Counting nt in col. j

Counting in j_1, j_2

$$s_i[j] = nt_j[\text{rank}(B_j, i)]$$

$$\Theta(1)$$

$$\Theta(r_j)$$

$$\Theta(\max(r_{j_1}, r_{j_2}))$$

Querying CREMSA

B

| | | | | | | | | | | | | | | | | | | | | | | | | | | | | |
|---|---|---|---|---|---|---|---|---|---|---|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|----|---|
| | 0 | 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 | 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 | 21 | 22 | 23 | 24 | 25 | 26 | |
| 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| 1 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 2 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 3 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |
| 4 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 |
| 5 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 | 0 |

The fewer runs, the faster the queries

nt

U
G

G
C

A
C

Accessing $s_i[j]$

Counting nt in col. j

Counting in j_1, j_2

$$s_i[j] = nt_j[\text{rank}(B_j, i)]$$

$$\Theta(1)$$

$$\Theta(r_j)$$

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Order of the sequences in the MSA matters

Fewer/longer runs lead to a lighter **and** quicker index

Order of the sequences in the MSA matters

Fewer/longer runs lead to a lighter **and** quicker index

```
GGUUUAUACCUUCGCAGGUAACAAACC  
GGUGUAUACCUUCCAGGUAACACACC  
GGUUUAUACCUUCCAGGUAACAACC  
GGUUUAUACCUUCGCAGGUAACAAACC  
GGUGUAUACCUUCGCAGGUAACACACC  
GGUGUAUACCUUCCAGGUAACACACC
```

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Fewer/longer runs lead to a lighter **and** quicker index

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GGUUUAUACCUUCGCAGGUAACAAACC  
GGUUUAUACCUUCGCAGGUAACAAACC  
GGUUUAUACCUUCCAGGUAACAAACC  
GGUGUAUACCUUCCAGGUAACACACC  
GGUGUAUACCUUCCAGGUAACACACC  
GGUGUAUACCUUCGCAGGUAACACACC
```

Order of the sequences in the MSA matters

Fewer/longer runs lead to a lighter **and** quicker index

```
11111111111111111111111111111111
00000000000000000000000000000000
00000000000000100000000000000000
000100000000000000000000000001000
000000000000000000000000000000000
00000000000000100000000000000000
GGUUUAUACCUUCGCAGGUAACAAACC
      G           C           C
                G
```

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Fewer/longer runs lead to a lighter **and** quicker index

```
11111111111111111111111111111111
00000000000000000000000000000000
00000000000000010000000000000000
000100000000000000000000000001000
000000000000000000000000000000000
00000000000000010000000000000000
GGUUUAUACCUUCGCAGGUAACAAACC
      G           C           C
                G
```

But finding the optimal order is NP-complete

CREMSA on 1M SARS-CoV-2 sequences

1,031,437 genomes

Downloaded in Dec 2023, deduplicated, removed those with ≥ 20 uncertain nucleotides

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Multiple sequence alignment

Using HAlign3, with 1.5 h CPU and **600 GB** of RAM. 36,000 columns

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CREMSA

| | |
|--------------|--------|
| Time | 10 min |
| RAM | 245 MB |
| Size on disk | 53 MB |

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Multiple sequence alignment

Using HAlign3, with 1.5 h CPU and **600 GB** of RAM. 36,000 columns

| | CREMSA | gzip | xz |
|--------------|--------|-----------|--------|
| Time | 10 min | 90 min | 70 min |
| RAM | 245 MB | 2 MB | 97 MB |
| Size on disk | 53 MB | 11,873 MB | 33 MB |

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Multiple sequence alignment

Using HAlign3, with 1.5 h CPU and **600 GB** of RAM. 36,000 columns

| | CREMSA | gzip | xz | CoMSA |
|--------------|--------|-----------|--------|-----------|
| Time | 10 min | 90 min | 70 min | 16 min |
| RAM | 245 MB | 2 MB | 97 MB | 63,266 MB |
| Size on disk | 53 MB | 11,873 MB | 33 MB | 9 MB |

CREMSA on 1M SARS-CoV-2 sequences

1,031,437 genomes

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Multiple sequence alignment

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| | CREMSA | gzip | xz | CoMSA |
|--------------|--------|-----------|--------|-----------|
| Time | 10 min | 90 min | 70 min | 16 min |
| RAM | 245 MB | 2 MB | 97 MB | 63,266 MB |
| Sorted input | 28 MB | | 24 MB | |
| Size on disk | 53 MB | 11,873 MB | 33 MB | 9 MB |

CREMSA on 1M SARS-CoV-2 sequences

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Multiple sequence alignment

Using HAlign3, with 1.5 h CPU and 600 GB of RAM. 36,000 columns

| | Index | CREMSA | Compressors | gzip | xz | CoMSA |
|--------------|-------|--------|-------------|-----------|--------|-----------|
| Time | | 10 min | | 90 min | 70 min | 16 min |
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| RAM | | 245 MB | 2 MB | 97 MB | 63,266 MB |
| Sorted input | | 28 MB | | 24 MB | |
| Size on disk | | 53 MB | 11,873 MB | 33 MB | 9 MB |
| Access | | 0.1 μ s | Compressors | | |
| Count | | 30 μ s | | | |
| Cons. score | | 40 μ s | | | |

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Multiple sequence alignment

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| RAM | | 245 MB | 2 MB | 97 MB | 63,266 MB |
| Sorted input | | 28 MB | | 24 MB | |
| Size on disk | | 53 MB | 11,873 MB | 33 MB | 9 MB |
| Access | | 0.1 μ s | Compressors | | |
| Count | | 30 μ s | | | |
| Cons. score | | 40 μ s | $\rightarrow \sim 6$ h for all the pairs of columns | | |

What conservation scores on 1M genomes tell us?

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Not much (yet)

Only 251 pairs have a good conservation score

Computing conservation scores on 1M genomes is great but...

What conservation scores on 1M genomes tell us?

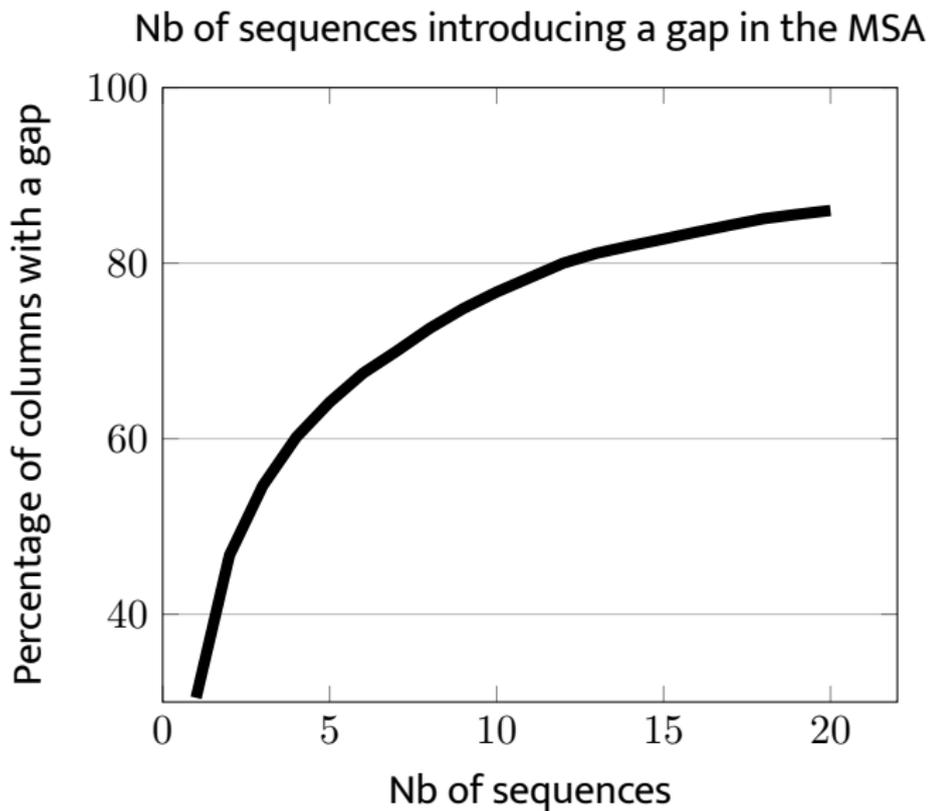
Not much (yet)

Only 251 pairs have a good conservation score

Computing conservation scores on 1M genomes is great but...

More data → more signal? **or** More data → more noise?

A few sequences introduce gaps in a column



CREMSA : Compressed indexing of (ultra) large viral alignments

<https://gitlab.univ-lille.fr/mikael.salson/cremsa>

CREMSA is fast and lightweight

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Reordering sequences save time and space

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Reordering sequences save time and space

Finding the optimal order is NP-hard

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CREMSA is fast and lightweight

Reordering sequences save time and space

Finding the optimal order is NP-hard

Conservation scores can be computed for 1M SARS-CoV-2

But we identified little interesting candidates

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Perspectives: Identify with CREMSA the sequences messing up the MSA

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Reordering sequences save time and space

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Conservation scores can be computed for 1M SARS-CoV-2

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Perspectives: Identify with CREMSA the sequences messing up the MSA

Side note: anyone interested to design a **lightweight** method for multiple sequence alignments of highly similar sequences?

Announcement: Open Maître de conférences position in Lille

Maître de conférences position open in Bonsai (CRISAL), Lille

Research themes in Bonsai

data structures, sequence algorithms, hash functions

oncohematology

non-ribosomal peptides

paleoproteomics

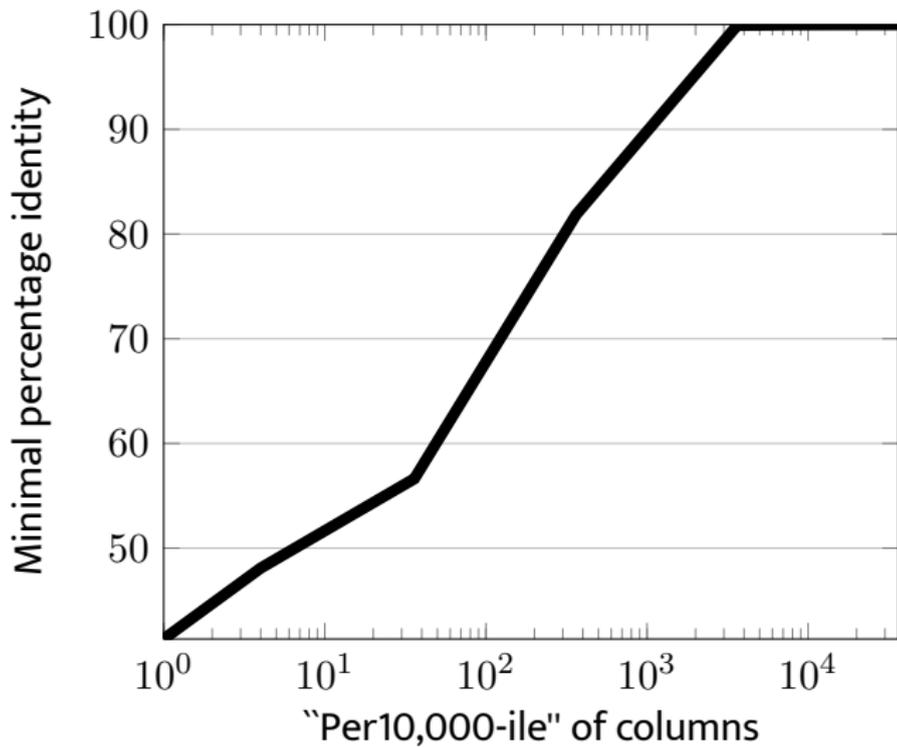
...

Contact me if interested: mikael.salson@univ-lille.fr

The 1M genomes are highly conserved

Percentage identity among the columns of the MSA

1,031,437 genomes



In practice r is tiny

r among the columns of the MSA
1,031,437 genomes

